An empirical wavelet transform-based approach for motion artifact removal in electroencephalogram signals

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\section{1. Introduction}

Electroencephalogram (EEG) quantitatively measures the human brain's electrical activity which takes place due to the firing of neurons \cite{1} and such brain activity is recorded non-invasively utilizing several electrodes located in different regions of the scalp \cite{2}. EEG is widely used to detect Alzheimer's disease \cite{3,4}, schizophrenia \cite{5,6}, sleep disorders \cite{7,8}, strokes \cite{9}, anaesthesia depth \cite{10} and cognitive impairment \cite{11,12}. EEG can also be used to detect epileptic seizures \cite{13-16}, human emotions \cite{17-19}, estimate drowsiness levels \cite{20,21} and develop brain–computer interfaces (BCIs) \cite{22-24}. EEG is a vital biological indicator; however, it is quite prone to motion artifacts caused by the voluntary or the involuntary movement of the patient while recording the EEG data. The measuring instruments are extremely sensitive and are susceptible to even movements as subtle as the blinking of eyes \cite{25}. Additionally, to obtain high-quality EEG data we require the impedance of the electrodes in contact with the skin to be sufficiently low \cite{26}. This is why traditionally data recording has required the use of conductive gel and proper skin preparation, but this approach is valid only for small durations since the gel dries out after a couple of hours \cite{26}. Recent advances have introduced dry electrodes but the quality of the signal recorded is degraded \cite{27,28}. Motion artifacts are the most devastating disturbances faced with dry electrodes and is the most important challenge yet to be addressed for the purpose of robust long term EEG monitoring \cite{26}.

These artifacts can hinder the performance of EEG-based systems \cite{25}. Primarily, there are 2 types of signal corrupting artifacts — physiological and the non-physiological. The physiological artifacts are introduced by the routine electrical activity of the body. These include those generated by the eyes, tongue, heart, muscles, and even sweat glands \cite{25}. The non-physiological artifacts are generated by the electromagnetic fields outside the body. Some examples of non-physiological artifacts are those introduced by the medical or data sampling instruments, 60 Hz artifact, electrode artifact \cite{25}. Therefore, it is important to suppress these artifacts. In this paper, we primarily focus on removing motion artifacts in EEG signals using the empirical wavelet transform (EWT) technique.

\textbf{Keywords:}
Empirical wavelet transform (EWT)
Motion artifact
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Electroencephalogram (EEG)
Principal component analysis
Noise removal

\textbf{A B S T R A C T}

Motion artifacts reduce the quality of information in the electroencephalogram (EEG) signals. In this study, we have developed an effective approach to mitigate the motion artifacts in EEG signals by using empirical wavelet transform (EWT) technique. Firstly, we decompose EEG signals into narrowband signals called intrinsic mode functions (IMFs). These IMFs are further processed to suppress the artifacts. In our first approach, principal component analysis (PCA) is employed to suppress the noise from these decomposed IMFs. In the second approach, the IMFs with noisy components are identified using the variance measure, which are then removed to obtain the artifact-suppressed EEG signal. Our experiments are conducted on a publicly available Physionet dataset of EEG signals to demonstrate the effectiveness of our approach in suppressing motion artifacts. More importantly, the IMF-variance-based approach has provided significantly better performance than the EWT-PCA based approach. Also, the IMF-variance based approach is computationally more efficient than the EWT-PCA based approach. Our proposed IMF-variance based approach achieved an average signal to noise ratio (\textit{A S N R}) of 28.26 dB and surpassed the existing methods developed for motion artifact removal.

\begin{thebibliography}{10}

\bibitem{1} T. Sunil Kumar

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Various methodologies have been explored in previous attempts to mitigate motion artifacts and eliminate noise from corrupted EEG signals. One such approach involves singular spectrum analysis (SSA) [29], which has been proposed for EEG denoising. In this method, SSA [30] is applied to decompose the single-channel EEG data, followed by the removal of motion-corrupted segments using adaptive noise cancellation (ANC).

Approaches outlined in [31–33] employ either empirical mode decomposition (EMD) or ensemble empirical mode decomposition (EEMD). EMD breaks down a signal into a finite and often small number of ‘intrinsic mode functions’ that allow well-behaved Hilbert transforms [32]. Approaches in [31–33] operate under the assumption that motion artifact information is present in either one or multiple sub-band signals. These sub-band signals are derived by decomposing the motion-corrupted EEG signal using time–frequency techniques. The decomposed sub-bands undergo processing to eliminate noise. Subsequently, these processed sub-band signals are combined to reconstruct a noise-suppressed EEG signal.

Sweeney et al. [31] employed various single-stage and two-stage techniques for removing motion artifacts, utilizing the discrete wavelet transform (DWT). DWT is a transformation that breaks down a given signal into several sets, where each set represents a time series of coefficients describing the signal’s time evolution in the corresponding frequency band [34,35]. Additionally, Sweeney et al. explored approaches such as empirical mode decomposition (EMD) cascaded with canonical correlation analysis (EMD-CCA) and ensemble empirical mode decomposition (EEMD) coupled with canonical correlation analysis (EEMD-CCA) [31]. These techniques involve the decomposition of single-channel EEG signals and use the autocorrelation function, along with a motion artifact-free reference signal, to identify and discard the corrupted components [36].

In another study [32], EMD, coupled with independent component analysis (ICA) referred to as EMD-ICA, was utilized. Independent component analysis is a statistical technique used for estimating independent components (ICs) by maximizing the non-Gaussianity of ICs, maximizing the likelihood of ICs, or minimizing mutual information between ICs [37]. Furthermore, EEMD was integrated with ICA (EEMD-ICA) to suppress motion artifacts from EEG in a different study [33].

In a recent study, Gajbhiye et al. [38] employed techniques grounded in multisolution total variation and multisolution weighted total variation to eradicate artifacts from EEG signals. Additionally, Gajbhiye et al. [39] utilized wavelet domain-optimized Savitzky–Golay filters for noise removal in EEG signals. The existing EMD-based approaches are computationally complex and take longer to implement than the EWT algorithm [40,41]. They also have drawbacks of mode mixing, iterative runs, and its requirement of the approach to determine the extreme points and stopping criteria [42]. To solve these significant sifting stopping criteria as standard deviation criterion [43], multi-threshold criterion, orthogonality criterion and bandwidth criterion [44] have been proposed. Albeit these criteria are not self-adaptive, we need to set the threshold to define the process which results in inconsistent performance based on the nature of the signal [42]. Similarly, even discrete wavelet transform (DWT) requires us to select the levels of decomposition manually [38]. The SSA method also requires manual selection of window length and number of components.

This paper attempts to solve these problems by using empirical wavelet transform (EWT) which is computationally more efficient than EMD and it is a self-adaptive technique [45]. The wavelets which are used to extract the intrinsic mode functions (IMFs) are tailor-made for each input signal rather than the selection of the wavelets from some prescribed dictionary. In DWT, the basis functions are fixed and do not change with the change in frequency information. EMD is an adaptive technique which adapts as per the change in frequency information. However, in EMD, there is no mathematical model and also the selection of stopping criteria is not well defined. Therefore, EWT is preferred over both the signal decomposition techniques as it is adaptive to frequency change and has a well-defined mathematical background. EWT has been extensively used for several applications such as noise suppression in speech signals, ECG signal contamination removal, denoising the vibration signals and recognizing the bearing faults, Ocular artifact removal using FBSE-EWT, Seismic noise attenuation using waveform classification [46–50].

A brief summary of the above discussion in the form of a qualitative comparison between our proposed method and other state of the art methods is presented in the Table 1. A more thorough and quantitative discussion between them is presented in Section 3.

The key highlights of the paper are as follows:

1. Developed EWT-based automated approaches for motion artifact suppression in EEG signals.
2. Explored two approaches namely, EWT–principal component analysis (PCA) based approach and IMF–variance based approach for artifact suppression.
3. IMF–variance based approach has outperformed existing approaches and found to be effective in motion artifact suppression.

2. Proposed methods

The block diagram in Figs. 1(a) and 1(b) present the proposed EWT-PCA and EWT-based denoising methods, respectively. The EEG signals are obtained from the publicly available Physionet database (detailed in Section 2.1). The Physionet database is quite robust and has only a few drawbacks such as the limited size of the dataset and the technical limitations of the EEG data acquisition system, since the entire dataset is acquired using the same equipment. The noisy EEG frames are identified using the trigger data provided with the EEG dataset. The decomposition of EEG signals are performed using EWT. For the EWT-PCA method, the first two principal components (PCs) of the IMF matrix are reconstructed to obtain the noise which is then subtracted from the artifact-contaminated EEG signal to obtain the denoised signal. For the EWT-based method, the variance of each IMF is calculated, and the two IMFs with the highest variance are set to zero. The denoised signal is then reconstructed from the remaining IMFs.

2.1. EEG database

The data used in this work was obtained from a publicly available Physionet database, specifically, the motion artifact contaminated fNIRS (functional Near Infrared Spectroscopy) EEG data [45,51]. The data consists of 23 different EEG signals recorded from the pre-frontal cortex. With a total of 2 recordings, one each from one of the 2 transducers. One transducer was disturbed to generate motion artifacts within 2-min intervals and the second one was kept undisturbed. The motion of the disturbed transducer was accurately recorded along with the lack of motion of the undisturbed second transducer by the use of the outputs of 3-axis accelerometers affixed to each transducer [45]. The accelerometer signals were digitally resampled at 2048 Hz to match the EEG signals [45].
Hence, there are two signals per EEG recording: one noisy signal containing motion artifacts and the other non-noisy reference signal. The comparison of the noisy signal with the reference signal reveals a high value of correlation coefficient in the time duration when the transducer was not manipulated, and a lower value of correlation was observed during the motion-contaminated intervals [45]. The non-motion contaminated signal is used as the reference to validate the proposed EWT-based denoising approach of the noisy signals.

The database mentions the frames of the signal containing motion artifact using trigger data which specifies the frames that contain the artifact. Using that data, we have isolated the frames containing motion artifacts. The signal was multiplied by 0.001 at all points since the database annotated that the gain of their amplifier was 1000 [45] to ensure the use of actual recordings. The noisy and reference signals for the second noisy frame of EEG1 (EEG1 represents the first EEG signal in the dataset) are shown in Fig. 2.

2.2. Method 1: EWT-based decomposition

Empirical wavelet transform (EWT) is applied to decompose the EEG signal [52]. It is an adaptive technique, typically used for analyzing non-stationary signals. Non-stationary signals have dynamically changing components i.e., no fixed period. To analyze and capture the information from the non-stationary signals, adaptive techniques are found to be more suitable when compared to non-adaptive techniques [53]. Discrete wavelet transform, Fourier transform are non-adaptive techniques as they have fixed basis functions which fails to capture varying information in the non-stationary signals.

EWT analyzes a signal by extracting or decomposing the signal into different frequency components or sub-bands of a signal. Firstly, the Fourier spectrum of the signal is computed. Then, the Fourier spectrum is segmented based on the information present in the form of frequency. Further, the adaptive filter banks are formed with help of the boundaries of the segments. Finally, these sub-bands are extracted
by designing wavelet filter banks customized for input signals. The subband refers to a signal which has a narrow frequency range in the Fourier spectrum and is centered around a specific frequency. Different sub-bands present in the input signal represent the narrow-band information at different locations of the frequency spectrum.

The adaptability of the wavelets is obtained by considering where the information is present in the spectrum of the analyzed signal [52] and then partitioning the Fourier spectrum accordingly. The major steps involved in EWT are as follows:

Firstly, the Fourier spectrum $X(\omega)$ is computed for the noisy input signal $x(n)$. Then $X(\omega)$ is partitioned to obtain the center frequencies ($f_1, f_2, \ldots, f_N$) by detecting the local maxima of the Fourier spectrum [46]. Thereafter, the boundaries are constructed by considering the neighboring center frequencies. Boundaries $\Omega_i$ can be present on the mid-points between two consecutive frequencies as:

$$\Omega_i = \left( f_{i-1} + f_i \right) / 2.$$  

(1)

After determining the boundaries, the approximation coefficients $W_0(1, t)$ and detailed coefficients $W_i(n, t)$ can be found using the scaling function $\phi_i(t)$ and the empirical wavelet function $\psi_i(\omega)$, respectively [46].

$$W_0(1, t) = F^{-1} \left( X(\omega) \phi_0(\omega) \right)$$  

(2)

$$W_i(n, t) = F^{-1} \left( X(\omega) \psi_i(\omega) \right)$$  

(3)

Here, $F^{-1}$ represents the inverse Fourier transform. The decomposition of the signal $x(n)$ into its IMFs is mathematically expressed as follows:

$$x(n) = \sum_{i=1}^{N} IMF_i$$  

(4)

where $N$ is the number of intrinsic modes obtained from EWT. The intrinsic mode functions can be obtained by convolving the scaling function $\phi_i(t)$ with the approximation coefficients $W_0(1, t)$ and empirical wavelet functions $\psi_i(t)$ with their corresponding detail coefficients $W_i(n, t)$ [46] as shown below:

$$IMF_1 = W_0(1, t) * \phi_0(t)$$  

(5)

$$IMF_n = W_i(n, t) * \psi_i(t), \forall n > 1$$  

(6)

2.3. Method 2: EWT-PCA-based denoising

Principal component analysis (PCA) is found to be effective in noise suppression of EEG signals [54]. Motivated by the success of PCA in noise suppression, we explore PCA along with EWT. In this work, PCA is applied to the IMFs obtained from (5–6). Each column in multiresolution analysis (MRA) represents one IMF. PCA isolates the orthogonal, uncorrelated components. The principal components (PCs) with the highest variance correspond to noise when the motion artifact has higher energy than the signal [55]. The signal reconstructed from the first two PCs of the second noisy frame of EEG 2 is shown in Fig. 2 (b).

Each IMF is standardized, and the covariance matrix ($Cov$) is calculated as follows:

$$IMF_i = \left( IMF_i - \mu_i \right) / \sigma_i$$  

(7)

$$Cov(i, j) = E \left( IMF_i \cdot IMF_j^T \right)$$  

(8)

where $\mu_i$ and $\sigma_i$ are the mean and standard deviation for $IMF_i$. The eigenvalues and eigenvectors are calculated for the covariance matrix. The $n$th PC, corresponding to the eigenvector with the $n$th highest eigenvalue is calculated as:

$$PC_n = E[I_{IMF}^T \cdot x_1^T]$$  

(9)

The PCs with the highest variance are retained and the remaining are discarded. In this work, we have retained the first two PCs to get reconstructed signal $x'(n)$. The denoised signal $x_\epsilon(n)$ is obtained by subtracting $x'(n)$ from the original noisy signal.

$$x'(n) = PC1 + PC2$$  

(10)

$$x_\epsilon(n) = x(n) - x'(n)$$  

(11)

2.4. IMF-variance based denoising

In general, the variance of IMFs with noise is high when compared to the variance of IMFs without noise [56]. Therefore, in this approach, the IMFs with the highest variance are set to zero to get the noise-suppressed signal.

Variance is calculated for each of the IMFs as follows:

$$Var_{inf} = \sum_{i=1}^{n} \left( IMF_i - \mu \right)^2$$  

(12)

here $n$ and $\mu$ represents the length, and mean of $IMF_i$, respectively. The two IMFs with the highest variance are removed, and the denoised signal is reconstructed using Eq. (4).

2.5. Performance metrics

To quantify the performance of our approach, we have explored three metrics namely, average signal to noise ratio ($\Delta SNR$), correlation coefficient ($\eta$) [28] and improvement in root mean square error (RMSE). The difference in signal-to-noise ratio (SNR) before and after applying the denoising technique is shown by $\Delta SNR$ and mathematically shown as:

$$\Delta SNR = SNR_{after} - SNR_{before}$$  

(13)

where $SNR_{before}$ and $SNR_{after}$ are defined as:

$$SNR_{before} = 10 \times \log \left( \frac{\|x_{ref}\|^2}{\|x_{ref} - x(n)\|^2} \right)$$  

(14)

$$SNR_{after} = 10 \times \log \left( \frac{\|x_{ref}\|^2}{\|x_{ref} - x_\epsilon(n)\|^2} \right)$$  

(15)

where $x_{ref}$ is the reference EEG.

The second metric, the percentage reduction in a correlation coefficient ($\eta$) is defined as follows:

$$\eta = \left[ 1 - \frac{1 - \rho_{after}}{1 - \rho_{before}} \right] \times 100$$  

(16)

where $\rho_{before} = \rho(x_{ref}, x(n))$ and $\rho_{after} = \rho(x_{ref}, x_\epsilon(n))$ are the correlation coefficients before and after removing the motion artifact.

The third metric is the improvement in RMSE. The RMSE before and after applying the denoising techniques are shown as follows:

$$RMSE = \frac{1}{N} \sum_{n=1}^{N} (x_{ref} - x(n))^2$$  

(17)

Where $x_i$ is the noisy or denoised signal and $x_{ref}$ is the reference signal. The improvement in RMSE is the difference between the RMSE of the noisy and denoised signal.

3. Results and discussions

We have evaluated the performance of the proposed EWT-PCA and EWT-based denoising techniques using all 23 EEGs in the database. The summary statistics of the results are provided in Table 2. The average value of $\Delta SNR$ and $\eta$ along with the deviation is 26.79 ± 3.10 dB and 52.92 ± 16.38%, respectively for the EWT-PCA-based denoising technique. Similarly, 28.26 ± 4.28 dB and 55.00 ± 13.08% are the average values of $\Delta SNR$ and $\eta$, respectively for the EWT-based denoising techniques.
Fig. 3. (a) Variation of $\Delta$SNR with the number of principal components retained. (b) Variation of $\eta$% with the number of principal components retained. (c) Variation of $\Delta$SNR with the number of high-frequency IMFs removed. (d) Variation of $\eta$ with the number of high-frequency IMFs removed.

The EWT-based denoising yielded better performance than the EWT-PCA-based EEG denoising, and also proved to be computationally more efficient.

The plot of $\Delta$SNR and $\eta$ with respect to the number of PCs is shown in Fig. 3(a-b). It can be seen that retaining more than two PCs improves the $\Delta$SNR value but $\eta$ value decreases. Therefore, due to this reason, the number of PCs is fixed to two. On the other hand, the plot of $\Delta$SNR and $\eta$ with respect to the number of high variance IMFs removed is shown in Fig. 3(c-d). It can be observed that removing 2 high-variance IMFs gave the best performance.

The motion artifact contaminated EEG signal, reference EEG signal, and denoised EEG signal are shown in Fig. 4 for EEG6 (EEG6 represents the sixth EEG signal in the dataset) for both proposed denoising methods. The motion artifacts are eliminated from the original noisy EEG signal. The $\Delta$SNR and $\eta$% values obtained for EEG6 are 27.24 dB and 66.01%, respectively using the EWT-PCA method. But the EWT-based method obtained the value of 27.92 dB and 67.88% for $\Delta$SNR and $\eta$, respectively.

For the proposed EWT-PCA denoising technique, the maximum value of $\Delta$SNR obtained was 33.72 dB for EEG5 and the maximum value of $\eta$ was 71.76% for EEG6. The minimum value of $\Delta$SNR obtained was 19.92 dB for EEG1 and the minimum value of $\eta$ was 29.09% for EEG15.

A quantitative comparison based on performance of the proposed EWT-based denoising technique along with the state-of-the-art methods developed for motion artifact removal from EEG signals are presented in Table 3. The proposed IMF-variance-based approach has the highest $\Delta$SNR among the approaches mentioned and has a comparable correlation coefficient percentage $\eta$ with only SSA-based denoising method with higher $\eta$%. However, it can be noted that the SSA-based denoising has a higher standard deviation implying the results given by it may have a high variance. The experimental results presented in this section demonstrate the effectiveness of the proposed approaches in suppressing motion artifacts in EEG signals.

For our future endeavors, we plan to perform our experiments on a larger EEG database. Also, we would like to explore the proposed approach in other research problems such as based brain–computer interfaces [59] and meal onset detection based on sound signals [60] where artifact suppression plays is essential. In addition, we plan to explore the power of EWT and advanced deep learning approaches such as...
Multi-Stage Temporal Convolutional Network for Action Segmentation (MS-TCN) \[61\] for artifact suppression.

4. Conclusions

In this paper, we have proposed the EWT-based approaches for the removal of motion artifacts from EEG signals. The proposed IMF-variance-based approach achieved an average $\triangle SNR$ and $\eta$ values of 28.26 dB and 55.00\%, respectively. Our experimental results suggest that the proposed approach can be employed to suppress the motion artifact noise in EEG signals. Our results also suggest that the IMF-variance-based approach is more effective in noise suppression than the EWT-PCA approach and the existing approaches in the literature.

Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Dr. Subrata Chakraborty (Co-Guest Editor, Emerging Trends in Healthcare Decision Support Systems)

Data availability

Public dataset.

References


